

**LESSON****9-9****Review for Mastery****The Quadratic Formula and the Discriminant**

The Quadratic Formula can be used to solve any quadratic equation.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Solve  $2x^2 - 5x - 12 = 0$  using the quadratic formula.**

$$2x^2 - 5x - 12 = 0$$

**Step 1:** Identify  $a$ ,  $b$ , and  $c$ .

$$a = 2$$

$$b = -5$$

$$c = -12$$

**Step 2:** Substitute into the quadratic formula.

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(2)(-12)}}{2(2)}$$

**Step 3:** Simplify.

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(2)(-12)}}{2(2)}$$

$$x = \frac{5 \pm \sqrt{25 - (-96)}}{4}$$

$$x = \frac{5 \pm \sqrt{121}}{4}$$

$$x = \frac{5 \pm 11}{4}$$

**Step 4:** Write two equations and solve.

$$x = \frac{5 + 11}{4} \quad \text{or} \quad x = \frac{5 - 11}{4}$$

$$x = 4 \quad \text{or} \quad x = -\frac{3}{2}$$

**Solve using the quadratic equation by filling in the blanks below.**

1.  $x^2 + 2x - 35 = 0$

$$a = \underline{\hspace{1cm}}; b = \underline{\hspace{1cm}}; c = \underline{\hspace{1cm}}$$

$$x = \frac{-\left(\boxed{\hspace{1cm}}\right) \pm \sqrt{\left(\boxed{\hspace{1cm}}\right)^2 - 4\left(\boxed{\hspace{1cm}}\right)\left(\boxed{\hspace{1cm}}\right)}}{2\boxed{\hspace{1cm}}}$$

Simplify:

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2.  $3x^2 + 7x + 2 = 0$

$$a = \underline{\hspace{1cm}}; b = \underline{\hspace{1cm}}; c = \underline{\hspace{1cm}}$$

$$x = \frac{-\left(\boxed{\hspace{1cm}}\right) \pm \sqrt{\left(\boxed{\hspace{1cm}}\right)^2 - 4\left(\boxed{\hspace{1cm}}\right)\left(\boxed{\hspace{1cm}}\right)}}{2\boxed{\hspace{1cm}}}$$

Simplify:

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3.  $x^2 + x - 20 = 0$

$$a = \underline{\hspace{1cm}}; b = \underline{\hspace{1cm}}; c = \underline{\hspace{1cm}}$$

$$x = \frac{-\left(\boxed{\hspace{1cm}}\right) \pm \sqrt{\left(\boxed{\hspace{1cm}}\right)^2 - 4\left(\boxed{\hspace{1cm}}\right)\left(\boxed{\hspace{1cm}}\right)}}{2\boxed{\hspace{1cm}}}$$

Simplify:

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4.  $2x^2 - 9x - 5 = 0$

$$a = \underline{\hspace{1cm}}; b = \underline{\hspace{1cm}}; c = \underline{\hspace{1cm}}$$

$$x = \frac{-\left(\boxed{\hspace{1cm}}\right) \pm \sqrt{\left(\boxed{\hspace{1cm}}\right)^2 - 4\left(\boxed{\hspace{1cm}}\right)\left(\boxed{\hspace{1cm}}\right)}}{2\boxed{\hspace{1cm}}}$$

Simplify:

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**LESSON****9-9****Review for Mastery****The Quadratic Formula and the Discriminant** *continued*

The discriminant of a quadratic equation is  $b^2 - 4ac$ . The discriminant will indicate the number of real solutions in a quadratic equation.

If $b^2 - 4ac > 0$	the equation has 2 real solutions.
If $b^2 - 4ac = 0$	the equation has 1 real solution.
If $b^2 - 4ac < 0$	the equation has 0 real solutions.

Find the number of real solutions of  $4x^2 - 8x + 5 = 0$  using the discriminant.

$$4x^2 - 8x + 5 = 0$$

**Step 1:** Identify  $a$ ,  $b$ , and  $c$ .

$$a = 4, b = -8, c = 5$$

**Step 2:** Substitute into  $b^2 - 4ac$ .

$$(-8)^2 - 4(4)(5)$$

**Step 3:** Simplify.

$$64 - 80 = -16$$

$b^2 - 4ac$  is negative.

There are no real solutions.

Find the number of real solutions of  $9x^2 - 49 = 0$  using the discriminant.

$$9x^2 - 49 = 0$$

**Step 1:** Identify  $a$ ,  $b$ , and  $c$ .

$$a = 9, b = 0, c = -49$$

**Step 2:** Substitute into  $b^2 - 4ac$ .

$$(0)^2 - 4(9)(-49)$$

**Step 3:** Simplify.

$$0 + 1764 = 1764$$

$b^2 - 4ac$  is positive.

There are two real solutions.

Find the number of real solutions of each equation using the discriminant by filling in the boxes below.

5.  $4x^2 + 20x + 25 = 0$

$$a = \boxed{\phantom{00}}; b = \boxed{\phantom{00}}; c = \boxed{\phantom{00}}$$

$$(\boxed{\phantom{00}})^2 - 4(\boxed{\phantom{00}})(\boxed{\phantom{00}})$$

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6.  $15x^2 + 8x - 1 = 0$

$$a = \boxed{\phantom{00}}; b = \boxed{\phantom{00}}; c = \boxed{\phantom{00}}$$

$$(\boxed{\phantom{00}})^2 - 4(\boxed{\phantom{00}})(\boxed{\phantom{00}})$$

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Find the number of real solutions of each equation using the discriminant.

7.  $x^2 + 9x - 36 = 0$

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8.  $25x^2 + 4 = 0$

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**LESSON****9-9****Practice A****The Quadratic Formula and the Discriminant****Solve using the quadratic formula.**

1.  $x^2 + 6x + 5 = 0$

a:  b:  c:

$$x = \frac{-\boxed{\phantom{00}} \pm \sqrt{\boxed{\phantom{00}}^2 - 4\boxed{\phantom{00}}\boxed{\phantom{00}}}}{2\boxed{\phantom{00}}}$$

2.  $x^2 - 9x + 20 = 0$

a:  b:  c:

$$x = \frac{-\boxed{\phantom{00}} \pm \sqrt{\boxed{\phantom{00}}^2 - 4\boxed{\phantom{00}}\boxed{\phantom{00}}}}{2\boxed{\phantom{00}}}$$

3.  $2x^2 + 9x + 4 = 0$

a:  b:  c:

4.  $x^2 - 3x - 18 = 0$

a:  b:  c:

**Find the number of real solutions of each equation using the discriminant.**

5.  $x^2 + 3x + 5 = 0$

6.  $x^2 + 10x + 25 = 0$

7.  $x^2 - 6x - 7 = 0$

$$b^2 - 4ac = \boxed{\phantom{00}}^2 - 4\boxed{\phantom{00}}\boxed{\phantom{00}} = \underline{\hspace{2cm}}$$

$$b^2 - 4ac = \boxed{\phantom{00}}^2 - 4\boxed{\phantom{00}}\boxed{\phantom{00}} = \underline{\hspace{2cm}}$$

$$b^2 - 4ac = \underline{\hspace{2cm}}$$

**Solve using any method.**

8.  $x^2 - 64 = 0$

9.  $x^2 + 12x + 36 = 0$

10.  $x^2 + 4x - 32 = 0$

11.  $2x^2 + 9x - 5 = 0$

**LESSON**  
**9-9****Practice B*****The Quadratic Formula and the Discriminant*****Solve using the quadratic formula.**

1.  $x^2 + x = 12$

2.  $4x^2 - 17x - 15 = 0$

3.  $2x^2 - 5x = 3$

4.  $3x^2 + 14x - 5 = 0$

**Find the number of real solutions of each equation using the discriminant.**

5.  $x^2 + 25 = 0$

6.  $x^2 - 11x + 28 = 0$

7.  $x^2 + 8x + 16 = 0$

**Solve using any method.**

8.  $x^2 + 8x + 15 = 0$

9.  $x^2 - 49 = 0$

10.  $6x^2 + x - 1 = 0$

11.  $x^2 + 8x - 20 = 0$

12. In the past, professional baseball was played at the Astrodome in Houston, Texas. The Astrodome has a maximum height of 63.4 m. The height of a baseball  $t$  seconds after it is hit straight up in the air with a velocity of 45 ft/s is given by  $h = -9.8t^2 + 45t + 1$ . Will a baseball hit straight up with this velocity hit the roof of the Astrodome? Use the discriminant to explain your answer.