

1 EXPLORE

Graphing $f(\theta) = \sin \theta$

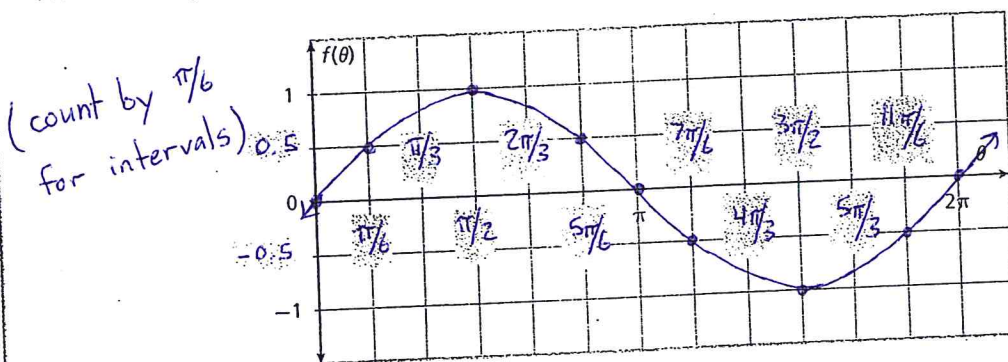
Mr. Ward

Graph $f(\theta) = \sin \theta$ for $0 \leq \theta \leq 2\pi$.

- A Complete the axis labels on the coordinate plane below. The θ -axis shows angle measures in radians. The $f(\theta)$ -axis shows the function values.
- B Complete the table of values.

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{2}$	$\frac{5\pi}{6}$	π	$\frac{7\pi}{6}$	$\frac{3\pi}{2}$	$\frac{11\pi}{6}$	2π
$f(\theta) = \sin \theta$	0	0.5	1	0.5	0	-0.5	-1	-0.5	0

- C Plot the points from the table and draw a smooth curve through them.



REFLECT

- 1a. Give a decimal approximation of $\sin \frac{\pi}{3}$. Check to see if the curve that you drew passes through the point $(\frac{\pi}{3}, \sin \frac{\pi}{3})$. What other points can you check based on the labeling of the θ -axis?

0.866, yes it is on the curve

other points to check: $\sin \frac{2\pi}{3}$, $\sin \frac{4\pi}{3}$, $\sin \frac{5\pi}{3}$

- 1b. On the interval $0 \leq \theta \leq 2\pi$, where does the sine function have positive values? Where does it have negative values?

Positive: $0 < \theta < \pi$ Negative: $\pi < \theta < 2\pi$

- 1c. List the θ -intercepts of the graph of $f(\theta) = \sin \theta$ on the interval $0 \leq \theta \leq 2\pi$. What do you think the next positive θ -intercept will be? Explain.

θ -intercepts: $0, \pi$, and 2π next at 3π (at multiples of π)

- 1d. What are the minimum and maximum values of $f(\theta) = \sin \theta$ on the interval $0 \leq \theta \leq 2\pi$? Where do the extreme values occur in relation to the θ -intercepts?

min = -1 max = 1 extreme values occur half way between the θ -intercepts

2 EXPLORE

Graphing $f(\theta) = \cos \theta$

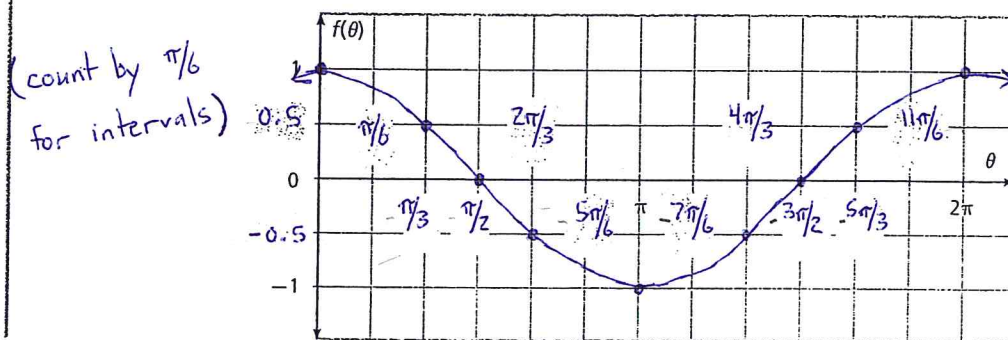
Mr. Ward

Graph $f(\theta) = \cos \theta$ for $0 \leq \theta \leq 2\pi$.

- A Complete the axis labels on the coordinate plane below. The θ -axis shows angle measures in radians. The $f(\theta)$ -axis shows the function values.
- B Complete the table of values.

θ	0	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	π	$\frac{4\pi}{3}$	$\frac{3\pi}{2}$	$\frac{5\pi}{3}$	2π
$f(\theta) = \cos \theta$	1	0.5	0	-0.5	-1	-0.5	0	0.5	1

- C Plot the points from the table and draw a smooth curve through them.



REFLECT

- 2a. On the interval $0 \leq \theta \leq 2\pi$, where does the cosine function have positive values?
Where does it have negative values?

Positive: $0 < \theta < \pi/2$ and $3\pi/2 < \theta < 2\pi$ Negative: $\pi/2 < \theta < 3\pi/2$

- 2b. List the θ -intercepts of the graph of $f(\theta) = \cos \theta$ on the interval $0 \leq \theta \leq 2\pi$.
What do you think the next positive θ -intercept will be? Explain.

θ -intercepts: $\pi/2$ and $3\pi/2$ next at $5\pi/2$ (odd multiples of $\pi/2$)

- 2c. What are the minimum and maximum values of $f(\theta) = \cos \theta$ on the interval $0 \leq \theta \leq 2\pi$? Where do the extreme values occur in relation to the θ -intercepts?

min = -1 max = 1 extreme values occur half way between the θ -intercepts